

QUADRATIC EQUATION

Q.1) The values of x satisfying the equation is

$$\frac{x-1}{x-2} + \frac{x-3}{x-4} = 3\frac{1}{3}; x \neq 2, 4$$

- (A) $3, \frac{3}{2}$ (B) $5, \frac{5}{2}$
(C) $7, \frac{7}{2}$ (D) $9, \frac{9}{2}$

Q.2) Which of the following equations has imaginary roots :

- (A) $x^2 - 4x + 2 = 0$ (B) $3x^2 + 2x - 1 = 0$
(C) $x^2 - 4x + 2 = 0$ (D) $x^2 + x + 1 = 0$

Q.3) If -4 is a root of the quadratic equation $x^2 + px - 4 = 0$ and the quadratic equation $x^2 + px + k = 0$ has equal roots, the value of k is

- (A) $\frac{3}{4}$ (B) $\frac{5}{4}$
(C) $\frac{7}{4}$ (D) $\frac{9}{4}$

Q.4) The values of k for which the equation $x^2 - 4x + k = 0$ has distinct real roots is

- (A) $k < 4$ (B) $k > 4$
(C) $k = 4$ (D) k is undefined

Q.5) A two digit number is four times the sum and three times the product of its digits. The number is

- (A) 22 (B) 23
(C) 24 (D) 25

Q.6) The quadratic equation whose roots are twice the roots of $2x^2 - 5x + 2 = 0$ is

- (A) $8x^2 - 10x + 2 = 0$ (B) $x^2 - 5x + 4 = 0$
(C) $2x^2 - 5x + 2 = 0$ (D) $x^2 - 10x + 6 = 0$

Q.7) If $c \neq 0$ and the equation $\frac{p}{2x} = \frac{a}{x+c} + \frac{b}{x-c}$ has two equal roots, then p can be

- (A) $(\sqrt{a} - \sqrt{b})^2$ (B) $(\sqrt{a} + \sqrt{b})^2$
(C) $a + b$ (D) $a - b$

Q.8) Out of a group of swans, $\frac{7}{2}$ times the square root of the total number of swans are on the bank of a pond. Two swans are in the water.

The total number of swans is?

- (A) 16 (B) 17
(C) 18 (D) 19

Q.9) If $x = \sqrt{1 + \sqrt{1 + \sqrt{1 + \dots \infty}}}$, then x is equal to

- (A) $\frac{1 + \sqrt{5}}{2}$ (B) $\frac{1 - \sqrt{5}}{2}$
(C) $\frac{1 \pm \sqrt{5}}{2}$ (D) $\frac{1 \pm \sqrt{3}}{2}$

Q.10) If one root of $5x^2 + 13x + k = 0$ is reciprocal of the other then $k =$

- (A) 0 (B) 5
(C) $\frac{1}{6}$ (D) 6

Q.11) If one of the roots of the quadratic equation is $2 + \sqrt{3}$ then find the quadratic equation.

- (A) $x^2 - (2 + \sqrt{3})x + 1 = 0$
(B) $x^2 + (2 + \sqrt{3})x + 1 = 0$
(C) $x^2 - 4x + 1 = 0$
(D) $x^2 + 4x - 1 = 0$

Q.12) Two candidates attempt to solve a quadratic equation of the form $x^2 + px + q = 0$. One starts with a wrong value of p and finds the roots to be 2 and 6. The other starts with a wrong value of q and finds the roots to be 2 and -9 . Find the correct roots of the equation:

- (A) 3, 4 (B) - 3, - 4
(C) 3, - 4 (D) - 3, 4
- Q.13)** Determine k such that the quadratic equation $x^2 + 7(3 + 2k) - 2x(1 + 3k) = 0$ has equal roots :
- (A) 2, 7 (B) 7, 5
(C) $2, -\frac{10}{9}$ (D) None of these
- Q.14)** The equation $x^2 - px + q = 0$, $p, q \in \mathbb{R}$ has no real roots if :
- (A) $p^2 > 4q$ (B) $p^2 < 4q$
(C) $p^2 = 4q$ (D) None of these
- Q.15)** Find the value of k such that the sum of the square of the roots of the quadratic equation $x^2 - 8x + k = 0$ is 40 :
- (A) 12 (B) 2
(C) 5 (D) 8
- Q.16)** Find the value of p for which the quadratic equation $x^2 + p(4x + p - 1) + 2 = 0$ has equal roots :
- (A) $-1, \frac{2}{3}$ (B) 3, 5
(C) $1, -\frac{4}{3}$ (D) $\frac{4}{3}, 2$
- Q.17)** The length of a hypotenuse of a right triangle exceeds the length of its base by 2 cm and exceeds twice the length of the altitude by 1 cm. Find the length of each side of the triangle (in cm) :
- (A) 6, 8, 10 (B) 7, 24, 25
(C) 8, 15, 17 (D) 7, 40, 41
- Q.18)** A plane left 40 minutes late due to bad weather and in order to reach its destination, 1600 km away in time, it had to increase its speed by 400 km/h from its usual speed. Find

the usual speed of the plane:

- (A) 600 km/h (B) 750 km/h
(C) 800 km/h (D) None of these
- Q.19)** The real values of a for which the quadratic equation $2x^2 - (a^3 + 8a - 1)x + a^2 - 4a = 0$ possesses roots of opposite signs are given by :
- (A) $a > 6$ (B) $a > 9$
(C) $0 < a < 4$ (D) $a < 0$
- Q.20)** The integral values of k for which the equation $(k - 2)x^2 + 8x + k + 4 = 0$ has both the roots real, distinct and negative is :
- (A) 0 (B) 2
(C) 3 (D) - 4
- Q.21)** If the roots of the equation $\frac{x^2 - bx}{ac - c} = \frac{m - 1}{m + 1}$ are equal and of opposite sign, then the value of m will be :
- (A) $\frac{a - b}{a + b}$ (B) $\frac{b - a}{a + b}$
(C) $\frac{a + b}{a - b}$ (D) $\frac{b + a}{b - a}$
- Q.22)** The values of k ($k > 0$) for which the equation $x^2 + kx + 64 = 0$ and $x^2 - 8x + k = 0$ both will have real roots is :
- (A) 8 (B) 16
(C) - 64 (D) None of these
- Q.23)** Solve : $\sqrt{2x + 9} - \sqrt{x - 4} = 3$
- (A) 4, 16 (B) 8, 20
(C) 2, 8 (D) None of these
- Q.24)** Solve $x : 6\left[x^2 + \frac{1}{x^2}\right] - 25\left(x + \frac{1}{x}\right) + 12 = 0$:
- (A) $-\frac{1}{3}, -\frac{1}{2}, 2, 3$ (B) $\frac{1}{3}, \frac{1}{2}, 2, 3$

(C) $\frac{1}{3}, \frac{1}{2}, -2, -3$ (D) None of these

Q.25) Solve for $x : 3^{x+2} + 3^{-x} = 10$

(A) $-3, -2$ (B) $-2, 0$
(C) $2, 3$ (D) None of these

Q.26) The sum of all the real roots of the equation

$$|x-2|^2 + |x-2|^2 - 2 = 0 \text{ is :}$$

(A) 2 (B) 3
(C) 4 (D) None of these

Q.27) If $a, b \in \{1, 2, 3, 4\}$, then the number of quadratic equation of the form $ax^2 + bx + 1 = 0$, having real roots is :

(A) 6 (B) 7
(C) 8 (D) None of these

Q.28) The number of real solutions of

$$x - \frac{1}{x^2 - 4} = 2 - \frac{1}{x^2 - 4} \text{ is :}$$

(A) 0 (B) 1
(C) 2 (D) Infinite

Q.29) The number of real roots of the equation $(x - 1)^2 + (x - 2)^2 + (x - 3)^2 = 0$:

(A) 0 (B) 2
(C) 3 (D) 6

Q.30) If both the roots of the equation $x^2 + mx + 1 = 0$ and $(b - c)x^2 + (c - a)x + (a - b) = 0$ are common then :

(A) $m = -2$ (B) $m = -1$
(C) $m = 0$ (D) $m = 1$

Answer Sheet

| | | | | | |
|------|---|------|---|------|---|
| Q.1 | B | Q.11 | C | Q.21 | A |
| Q.2 | D | Q.12 | B | Q.22 | B |
| Q.3 | D | Q.13 | C | Q.23 | B |
| Q.4 | A | Q.14 | B | Q.24 | A |
| Q.5 | B | Q.15 | A | Q.25 | B |
| Q.6 | B | Q.16 | A | Q.26 | C |
| Q.7 | B | Q.17 | C | Q.27 | B |
| Q.8 | A | Q.18 | C | Q.28 | A |
| Q.9 | A | Q.19 | C | Q.29 | A |
| Q.10 | B | Q.20 | C | Q.30 | A |